

# PhD lightning talk

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Christophe Gabreau, Mélanie Ducoffe AIRBUS



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①

**PhD context**  
**Vision based landing system**

②

**PhD Subject**  
**Formal verification of high dimension  
ML based systems**





# Context

- ① Context
- ② Subject





# Landing phase

Buenos Aires - Argentina



You

Danny





# Landing phase

Buenos Aires - Argentina



## Runway position

- 1- longitude
- 2- latitude
- 3- altitude



## Aircraft position

- 1- longitude
- 2- latitude
- 3- altitude

## Aircraft inclinaison

- 1- yaw
- 2- pitch
- 3- roll



You

Danny





# Landing phase

Buenos Aires - Argentina



## Runway position

- 1- longitude Known
- 2- latitude Known
- 3- altitude Known



## Aircraft position

- 1- longitude Known
- 2- latitude Known
- 3- altitude Known

## Aircraft inclinasion

- 1- yaw
- 2- pitch
- 3- roll



You

Danny





# Landing phase

Buenos Aires - Argentina



## Runway position

- 1- longitude Known
- 2- latitude Known
- 3- altitude Known



## Aircraft position

- 1- longitude Known
- 2- latitude Known
- 3- altitude Known

## Aircraft inclinasion

- 1- yaw Known
- 2- pitch Known
- 3- roll **Unknown**



You

Danny





# Landing phase

Buenos Aires - Argentina



Danny





# Landing phase

Buenos Aires - Argentina



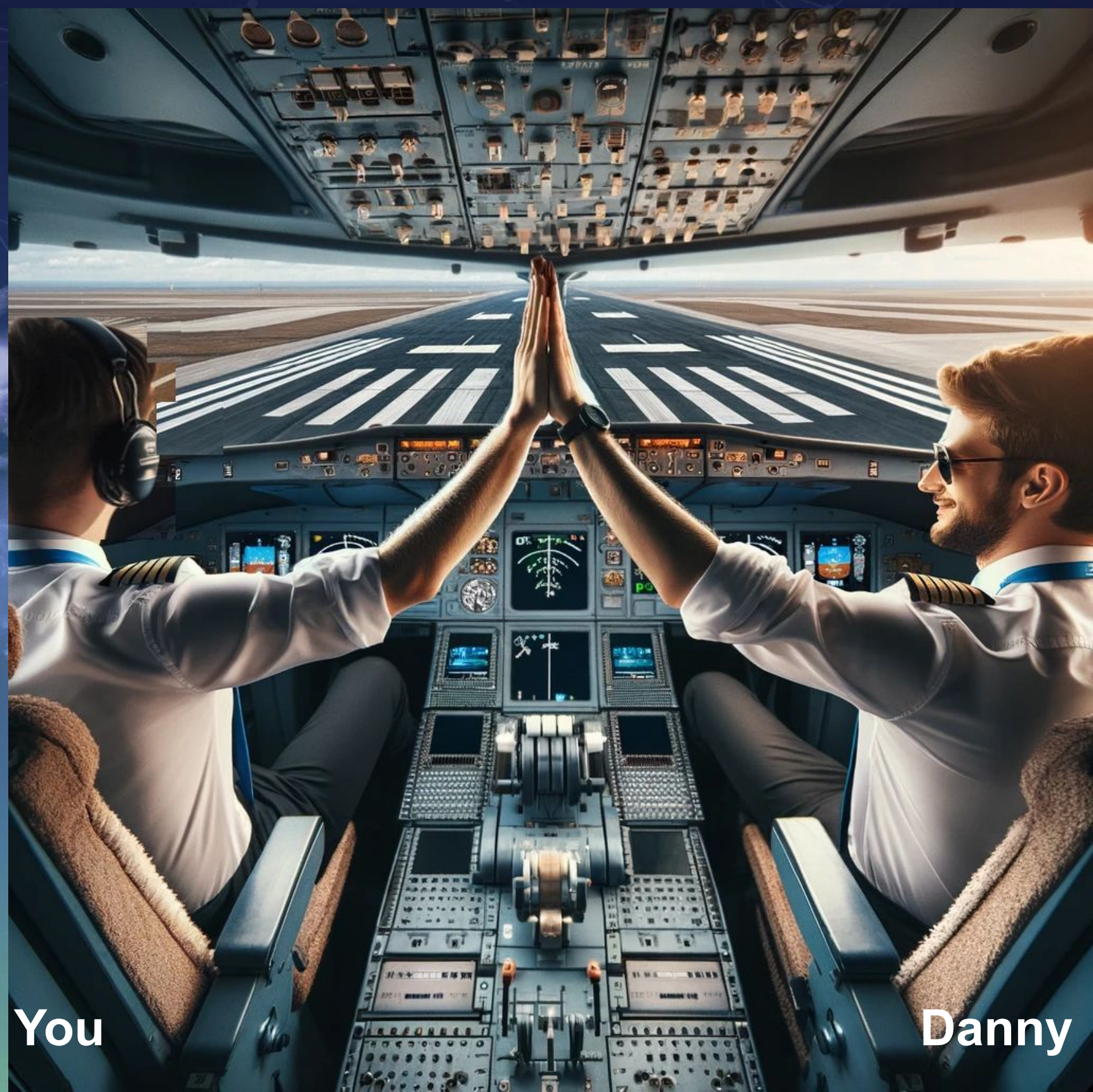
Danny





# Successful landing

Buenos Aires - Argentina



You

Danny





# After landing

Buenos Aires - Argentina



You

Danny

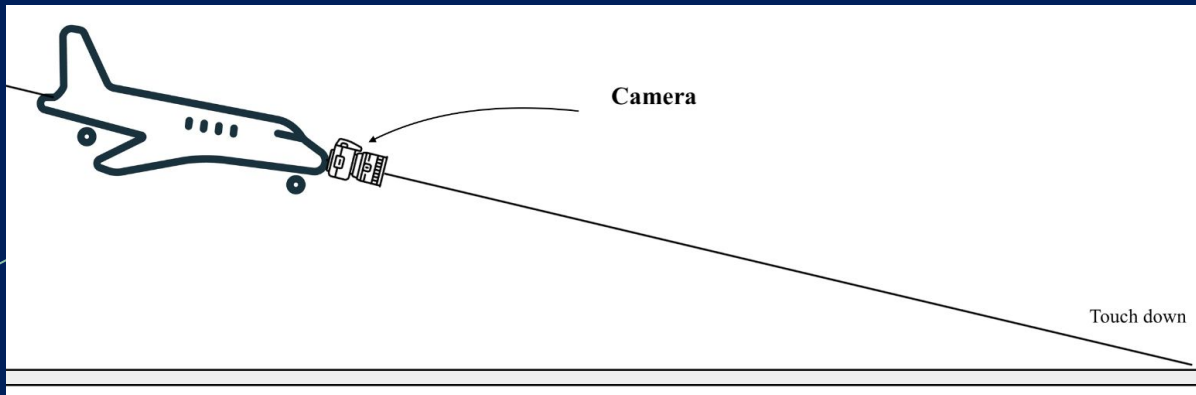




# After landing

Buenos Aires - Argentina

What if we added redundant "roll" function with a camera ?



You

Danny





# After landing

Buenos Aires - Argentina



You

Danny





# After landing

Buenos Aires - Argentina



You

Danny





# After landing

Buenos Aires - Argentina



You

Danny





# After landing

Buenos Aires - Argentina



Classical algorithm

Roll



You

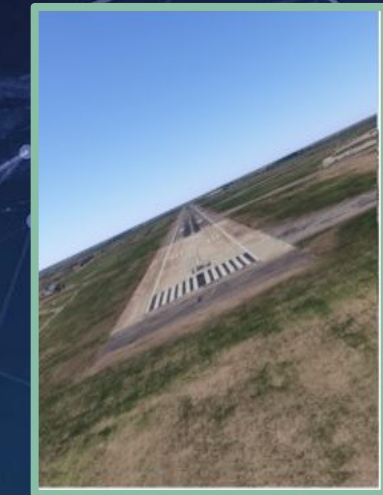
Danny





# After landing

Buenos Aires - Argentina



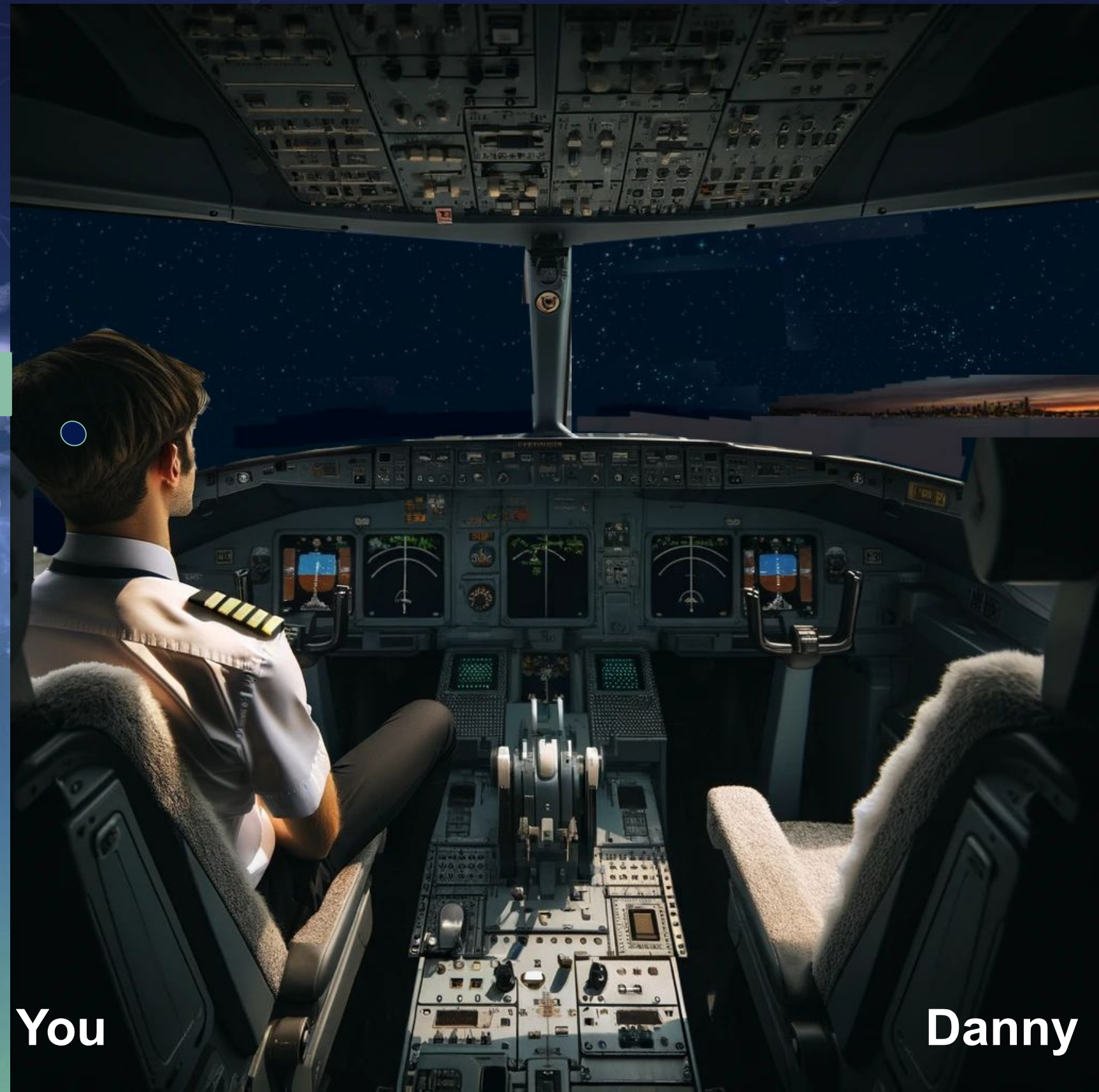
ML model



Classical algorithm

Roll

How can we certify this machine learning model?



You

Danny





**Subject**

- ① Context
- ② Subject



**Subject**



- ① Context
- ② Subject



**Subject**  
**Formal method**



① **Context**

② **Subject**



**Neural network**



**Property**



**Pre/Post conditions**



**Formalized property**



**Verification tools**





# Neural network

Successive image transformations

① **Context**

② **Subject**



**Neural network**



**Property**



**Pre/Post-conditions**



**Formalized property**



**Verification tools**

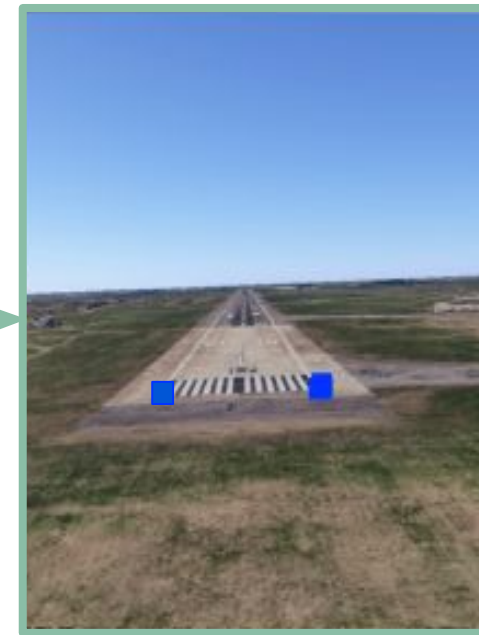
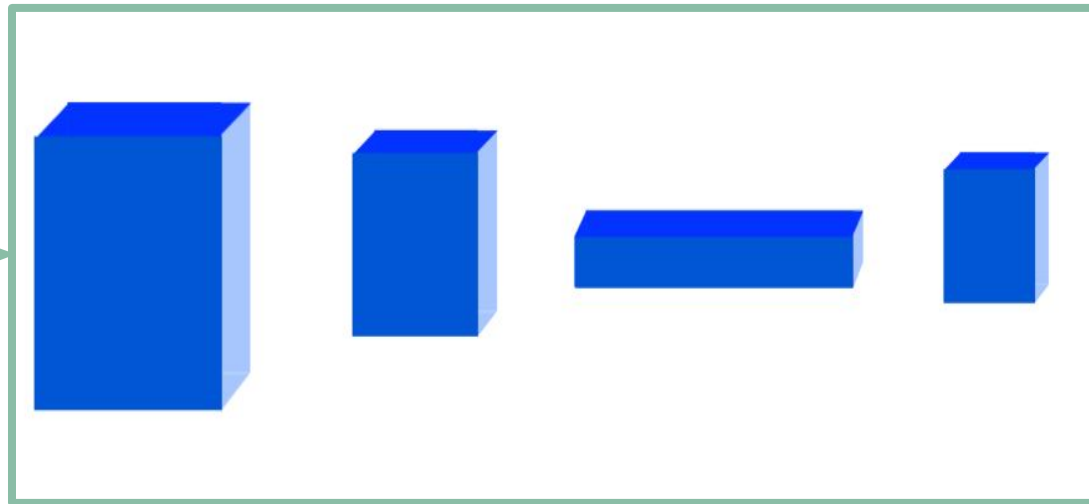




# Neural network

## Successive image transformations

### Machine learning model



① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

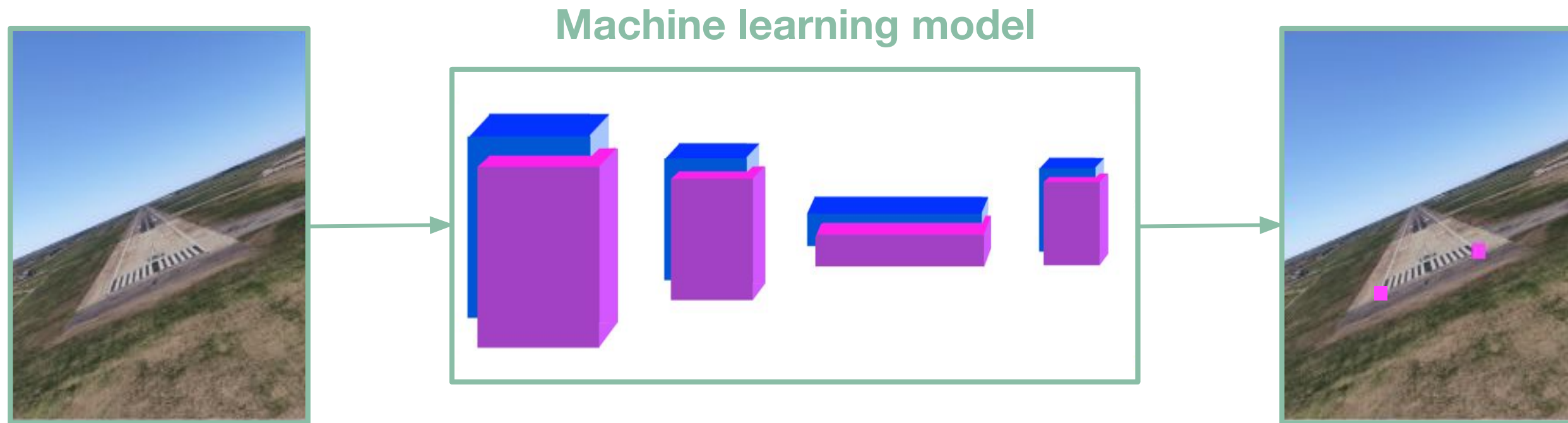
 Verification tools





# Neural network

Successive image transformations



① **Context**

② **Subject**

 **Neural network**

 **Property**

 **Pre/Post-conditions**

 **Formalized property**

 **Verification tools**





# Property

Requirement on desired model behavior

① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

 Verification tools





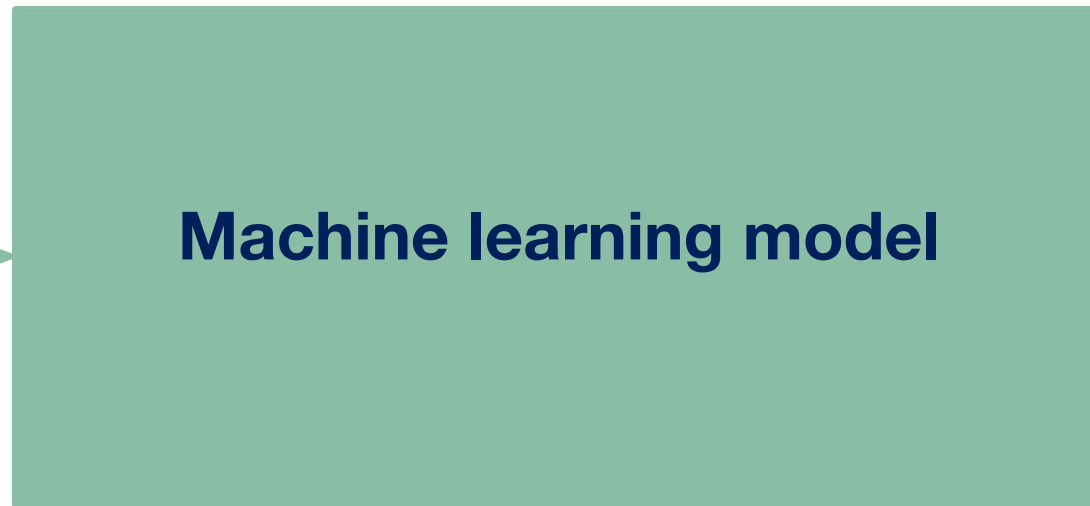
# Property

Requirement on desired model behavior

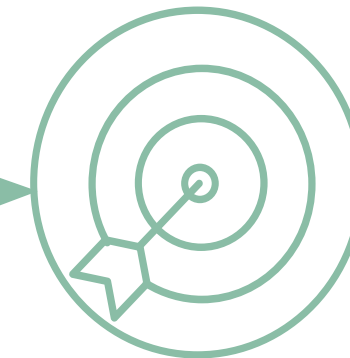
**Pre-condition**



Neural network  
input constraints



**Post-condition**



Neural network  
output constraints

① **Context**

② **Subject**

 Neural network

 **Property**

 Pre/Post-conditions

 Formalized property

 Verification tools





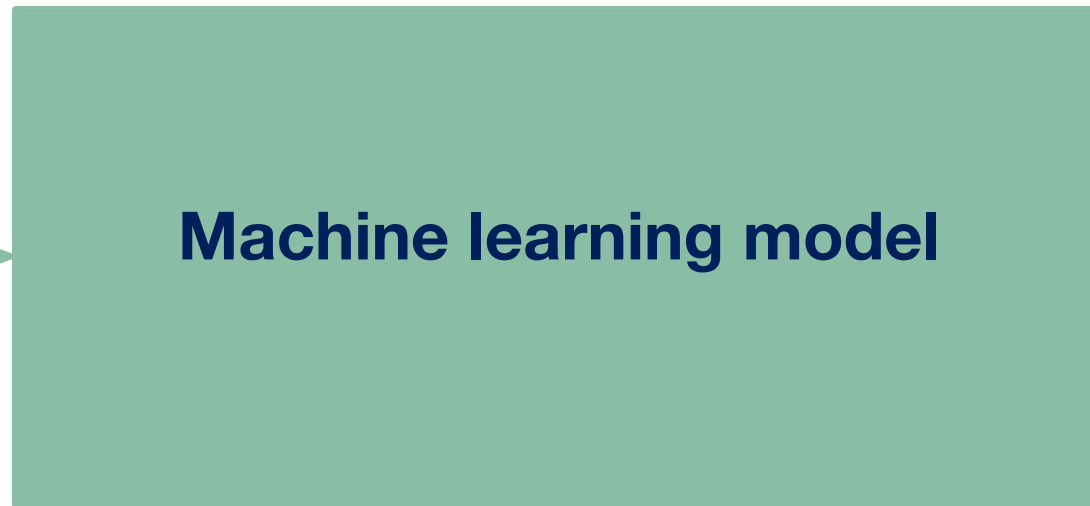
# Property

Requirement on desired model behavior

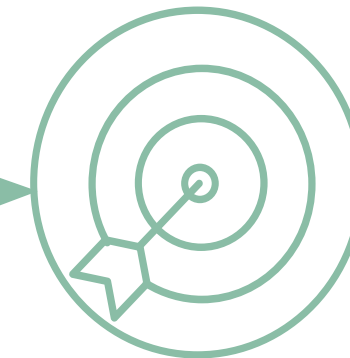
**Pre-condition**



Neural network  
input constraints



**Post-condition**



Neural network  
output constraints

If the input meets the pre-condition, then,  
the output meets the post-condition

① **Context**

② **Subject**

 Neural network

 **Property**

 Pre/Post-conditions

 Formalized property

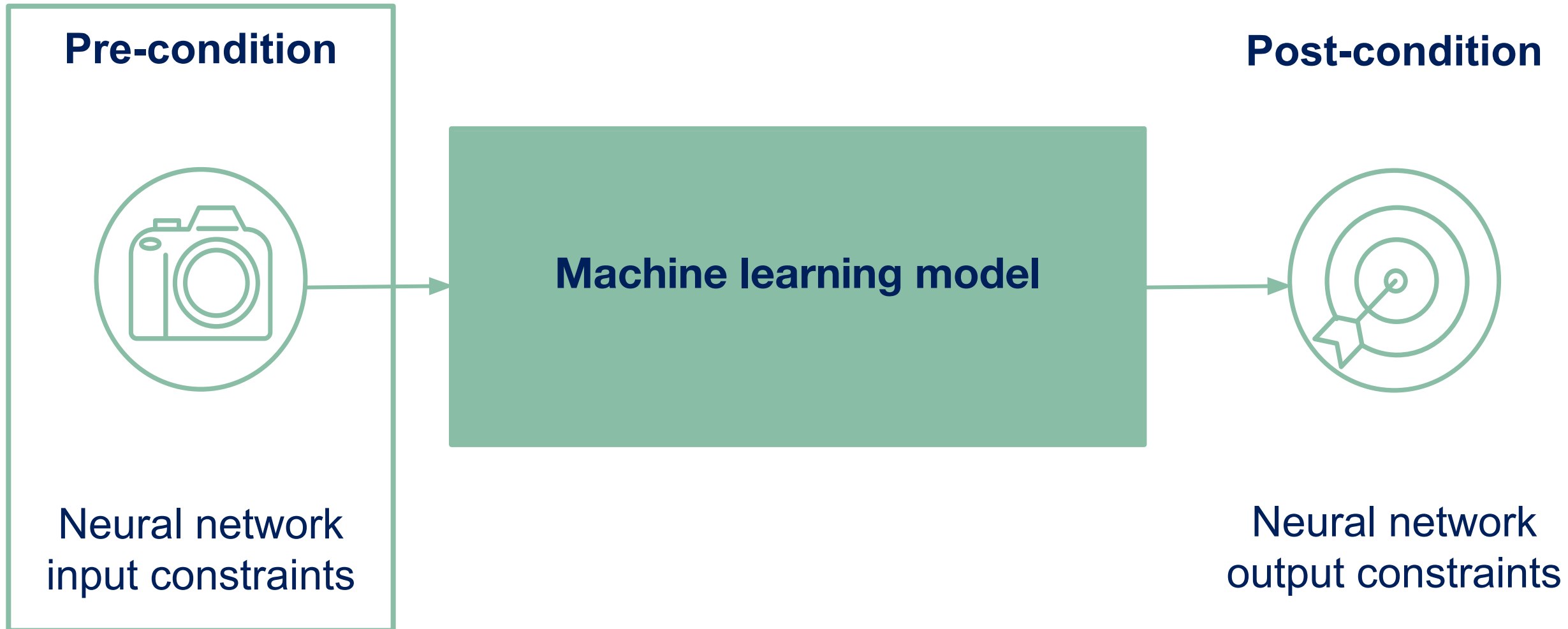
 Verification tools





# Pre-conditions

Neural network input constraints



① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

 Verification tools





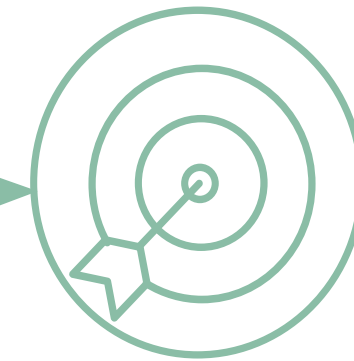
# Pre-conditions

## Neural network input constraints



Machine learning model

Post-condition



Neural network  
output constraints

① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

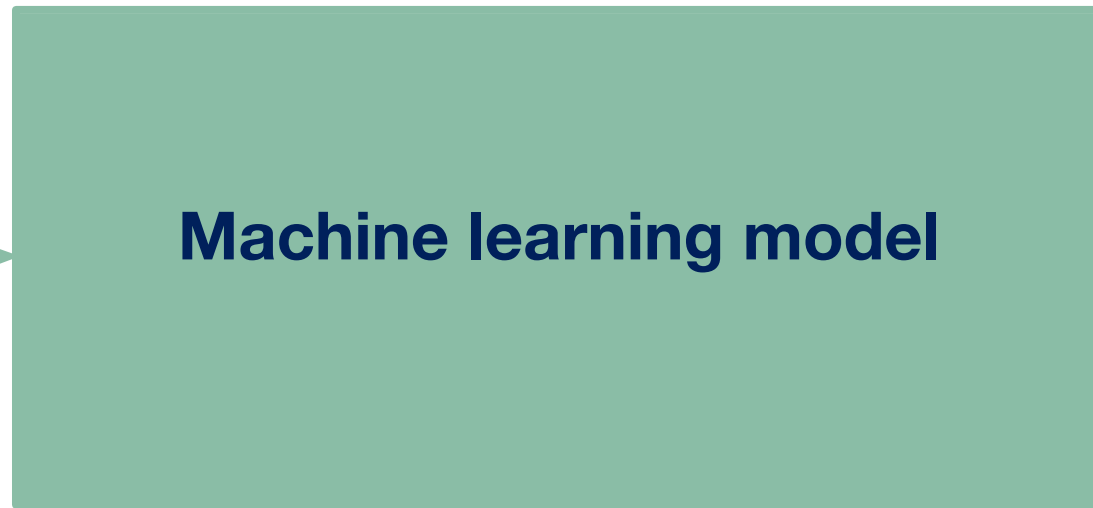
 Verification tools



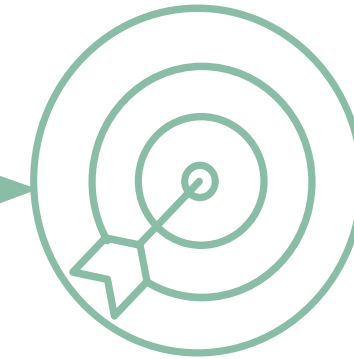


# Pre-conditions

## Neural network input constraints



## Post-condition



## Neural network output constraints



### Runway position

- 1- longitude 58.534
- 2- latitude 34.804
- 3- altitude 0 m



### Aircraft position

- 1- longitude 58.534
- 2- latitude 34.807
- 3- altitude 25 m

### Aircraft inclinasion

- 1- yaw 0
- 2- pitch 86°
- 3- roll 0



### Environmental conditions

Weather: Sunny

Airport: Buenos Aires  
Grass  
No building

① Context

② Subject



Neural network



Property



Pre/Post-conditions



Formalized property



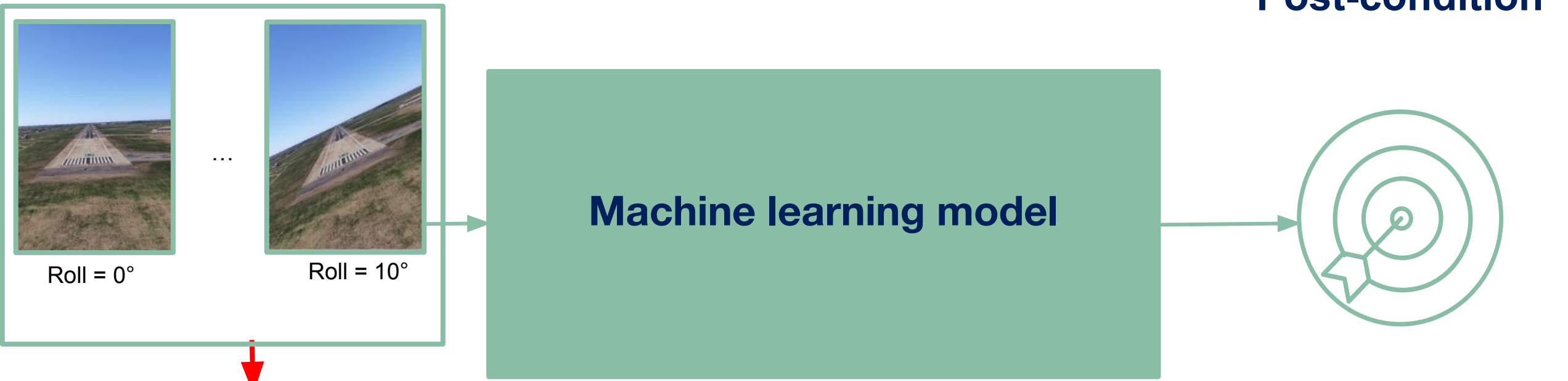
Verification tools





# Pre-conditions

## Neural network input constraints



**Runway position**

1- longitude	58.534
2- latitude	34.804
3- altitude	0 m

**Aircraft position**

1- longitude	58.534
2- latitude	34.807
3- altitude	25 m

**Aircraft inclinasion**

1- yaw	0
2- pitch	86°
3- roll	∈ [0°, 10°]

**Environmental conditions**

Weather: Sunny

Airport: Buenos Aires  
Grass  
No building

Neural network output constraints

- ① Context
- ② Subject
- Neural network
- Property
- Pre/Post-conditions**
- Formalized property
- Verification tools

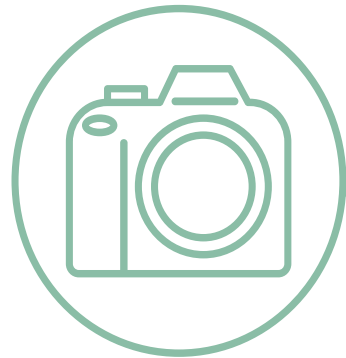




# Post-conditions

Desired model behavior

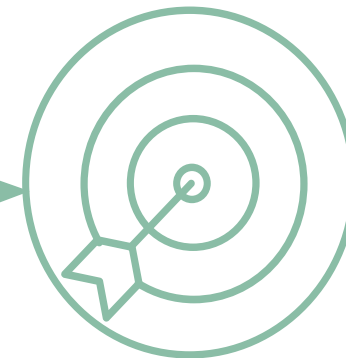
**Pre-condition**



Neural network  
input constraints

**Machine learning model**

**Post-condition**



Neural network  
output constraints

① **Context**

② **Subject**

 Neural network

 Property

 **Pre/Post-conditions**

 Formalized property

 Verification tools

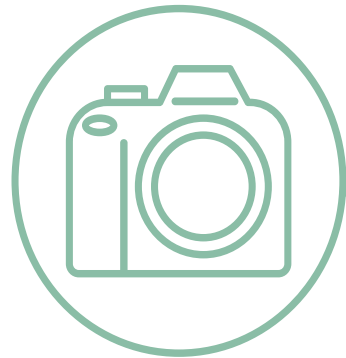




# Post-conditions

Desired model behavior

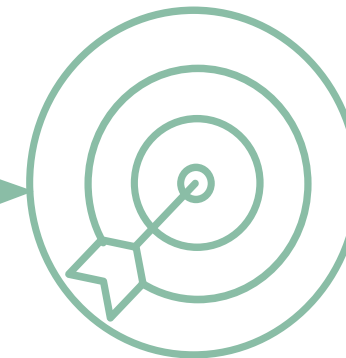
## Pre-condition



Neural network  
input constraints

Machine learning model

## Post-condition



Neural network  
output constraints

Defined by:

- Business requirements
- Technical constraints
- Performance
- ...

① **Context**

② **Subject**

 Neural network

 Property

 **Pre/Post-conditions**

 Formalized property

 Verification tools





# Post-conditions

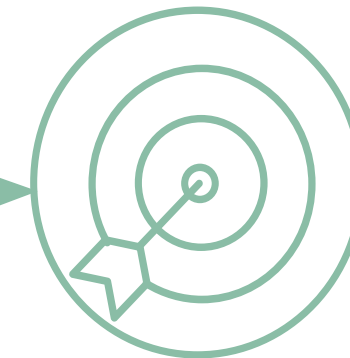
Desired model behavior

Pre-condition



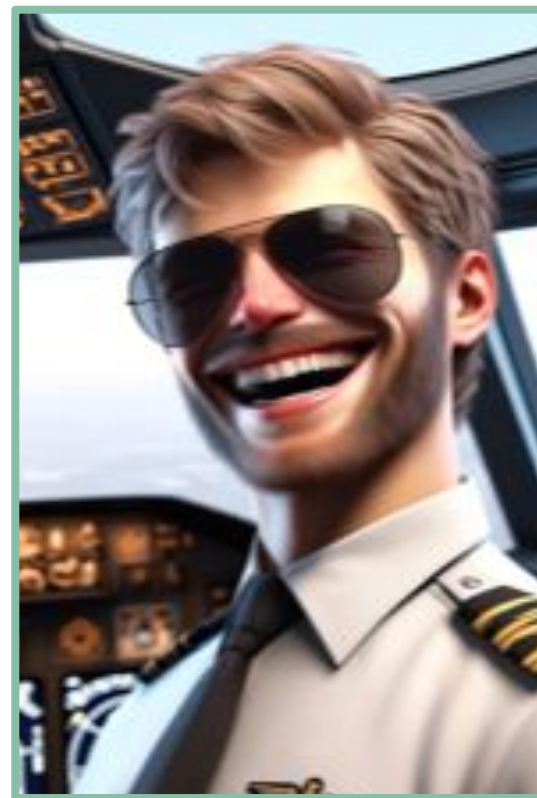
Machine learning model

Post-condition



Neural network  
input constraints

Neural network  
output constraints



Danny

Defined by:

Business requirements

- Technical constraints
- Performance
- ...

① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

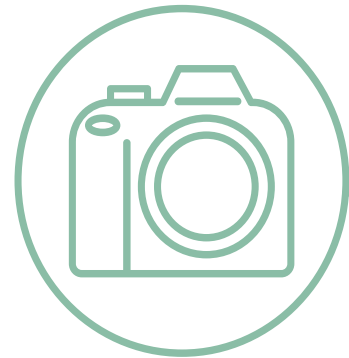
 Verification tools



# Post-conditions

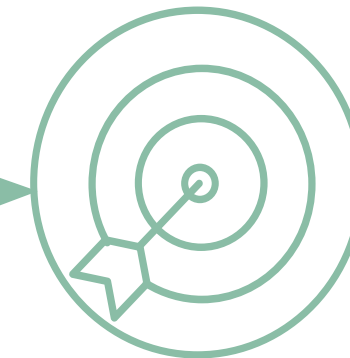
Desired model behavior

Pre-condition



Machine learning model

Post-condition



Neural network  
input constraints

Neural network  
output constraints

Delimited zone



① Context

② Subject



Neural network



Property



Pre/Post-conditions



Formalized property



Verification tools





# Formalized property

## Mathematical traduction

① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

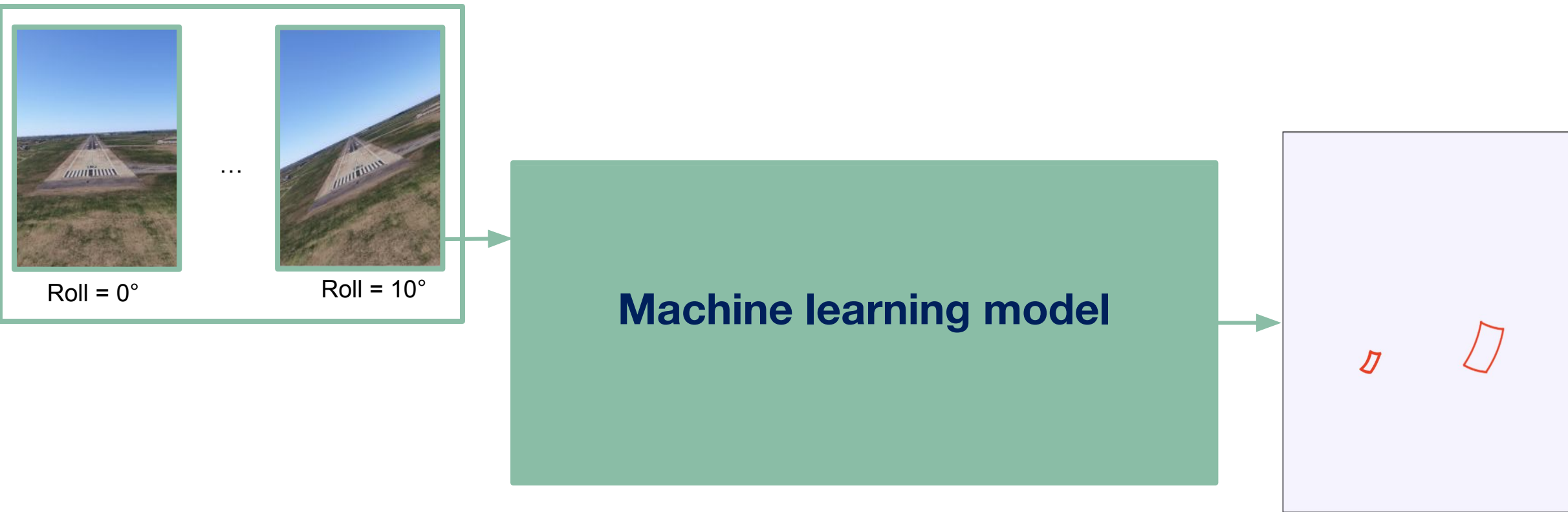
 **Formalized property**

 Verification tools



# Formalized property

Mathematical traduction



① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

 **Formalized property**

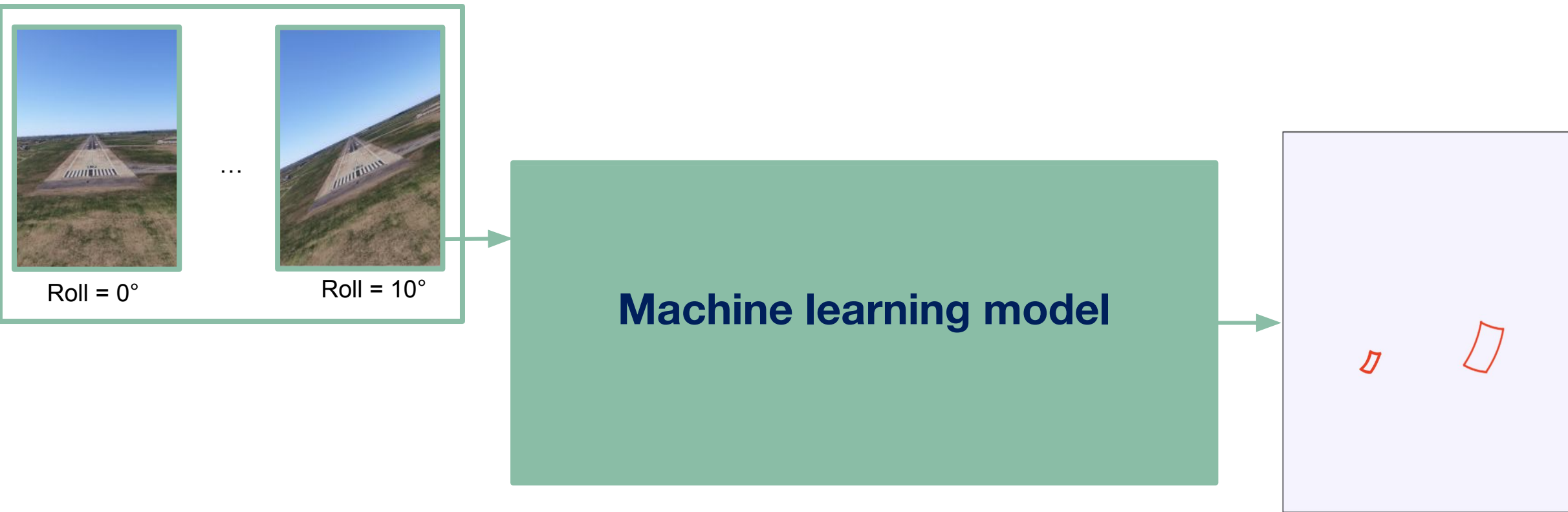
 Verification tools





# Formalized property

Mathematical traduction



What does it means mathematically :  
“The input meets the precondition”?

① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

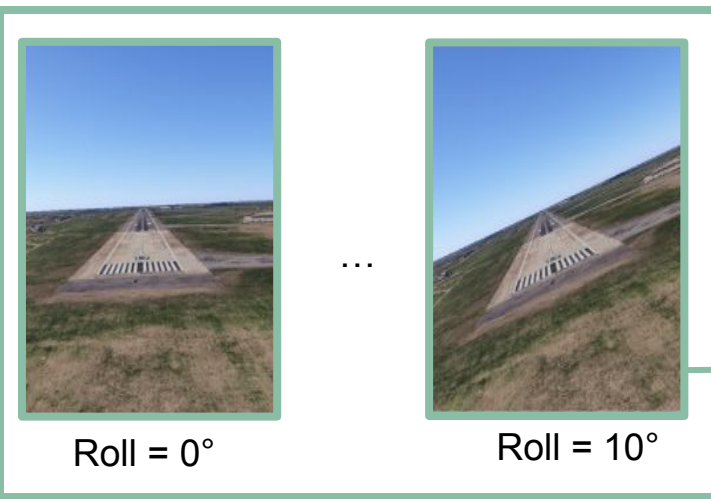
 **Formalized property**

 Verification tools

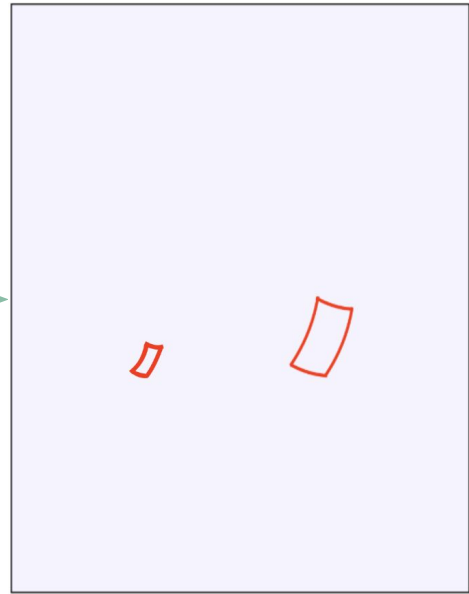


# Formalized property

Mathematical traduction



**Machine learning model**



1	2	3
4	5	6
7	8	9

9 pixels image

① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

 **Formalized property**

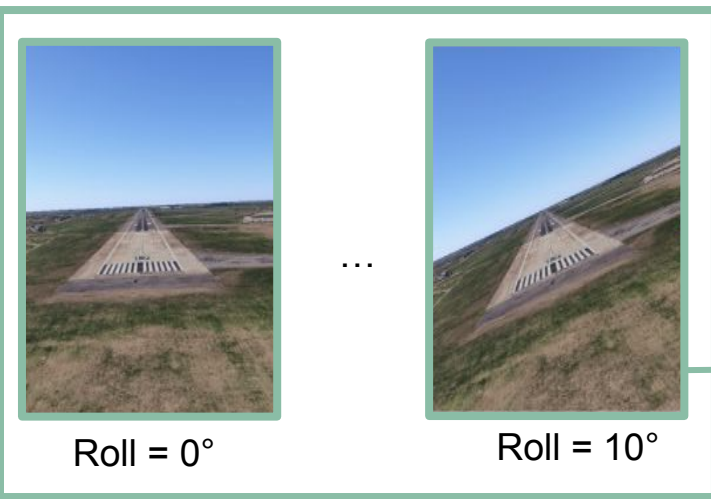
 Verification tools



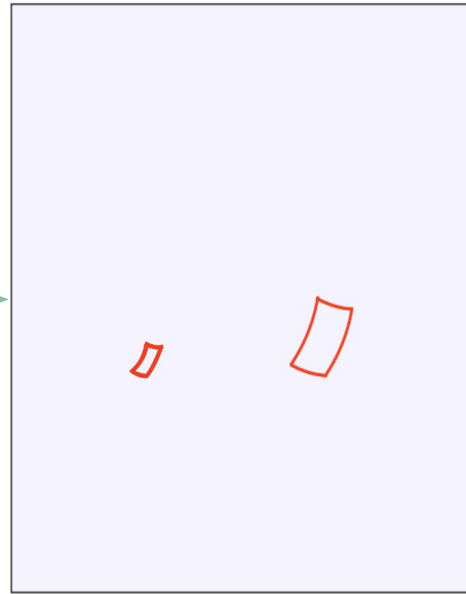


# Formalized property

Mathematical traduction



**Machine learning model**



1	2	3
4	5	6
7	8	9

■	■	
	■	

example

- ① Context
- ② Subject

Neural network

Property

Pre/Post-conditions

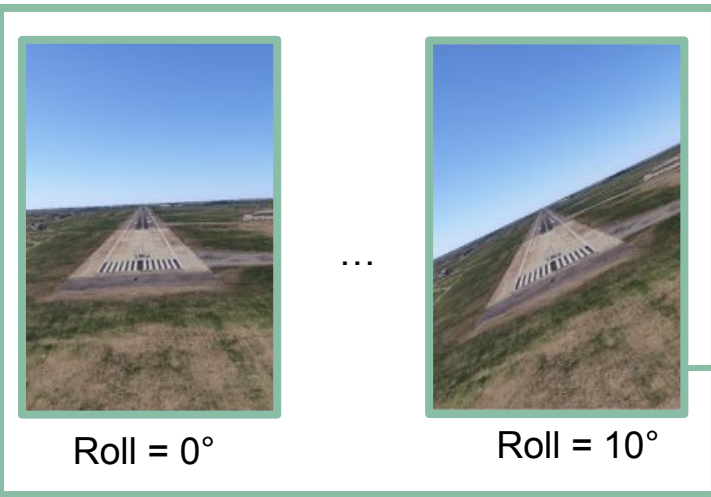
Formalized property

Verification tools

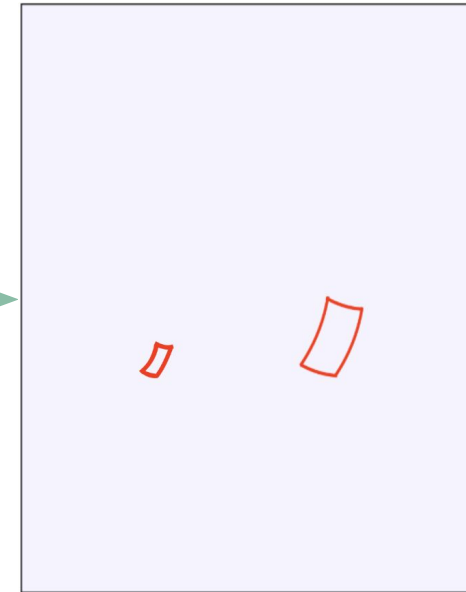


# Formalized property

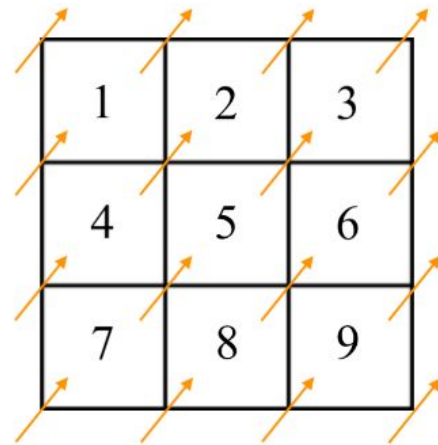
## Mathematical traduction



**Machine learning model**



1	2	3
4	5	6
7	8	9



■	■	
	■	

example

① **Context**

② **Subject**

Neural network

Property

Pre/Post-conditions

**Formalized property**

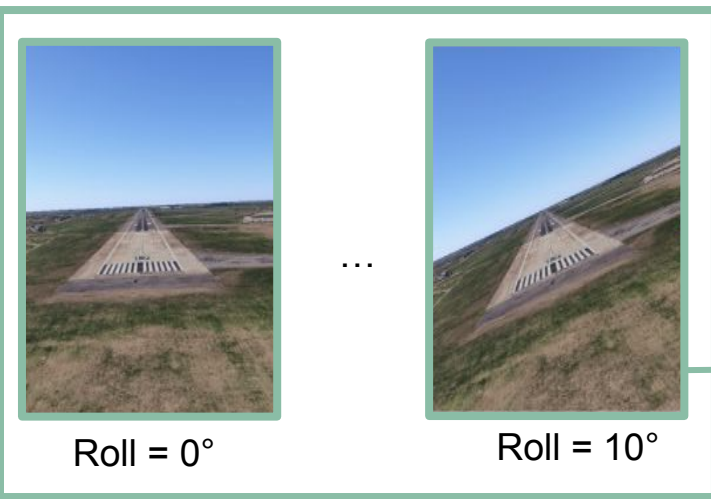
Verification tools



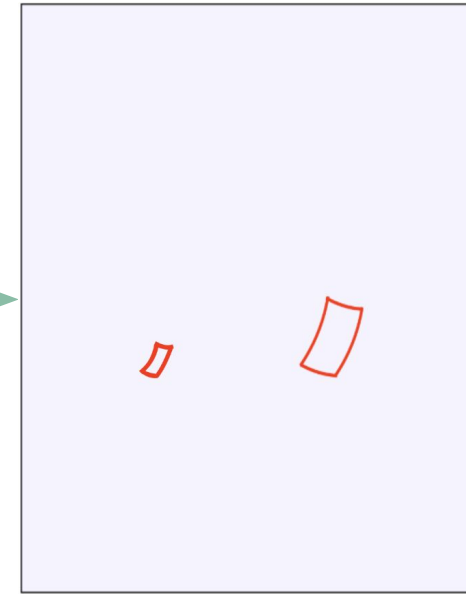


# Formalized property

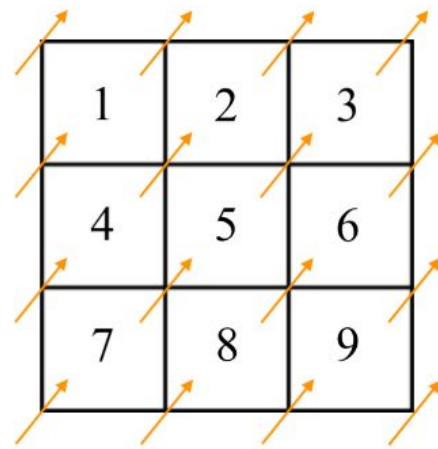
## Mathematical traduction



**Machine learning model**



1	2	3
4	5	6
7	8	9



?	4	5
?	7	8
?	?	?

■	■	
	■	

example

■	■	■
■		■
■	■	■

example

① Context

② Subject

Neural network

Property

Pre/Post-conditions

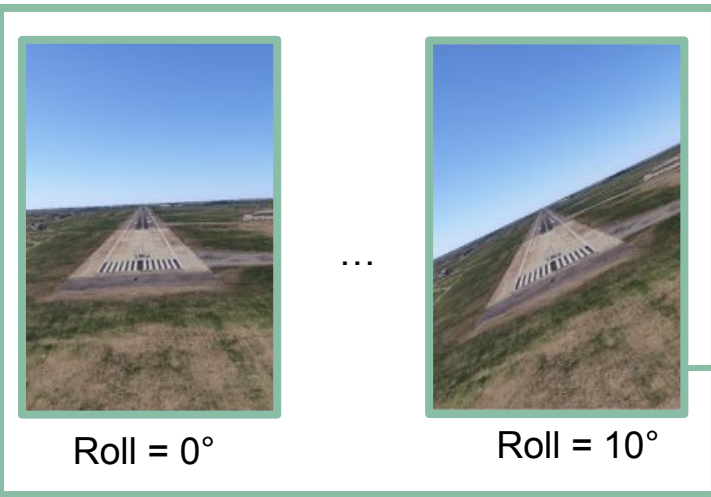
Formalized property

Verification tools

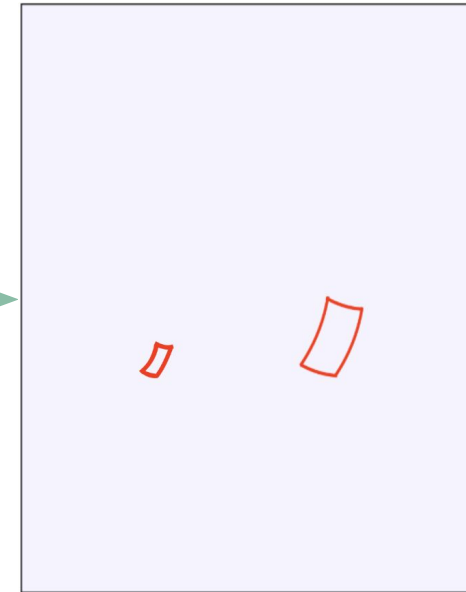


# Formalized property

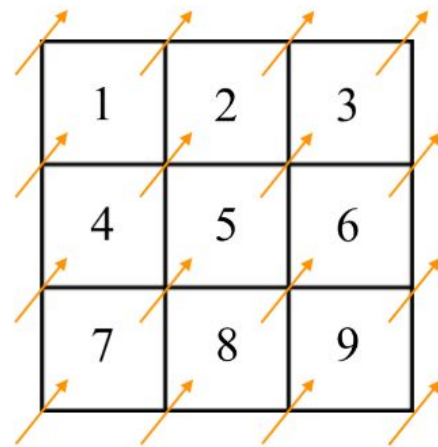
## Mathematical traduction



**Machine learning model**



1	2	3
4	5	6
7	8	9



?	4	5
?	7	8
?	?	?

5 pixels unknown in black and white

① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

 **Formalized property**

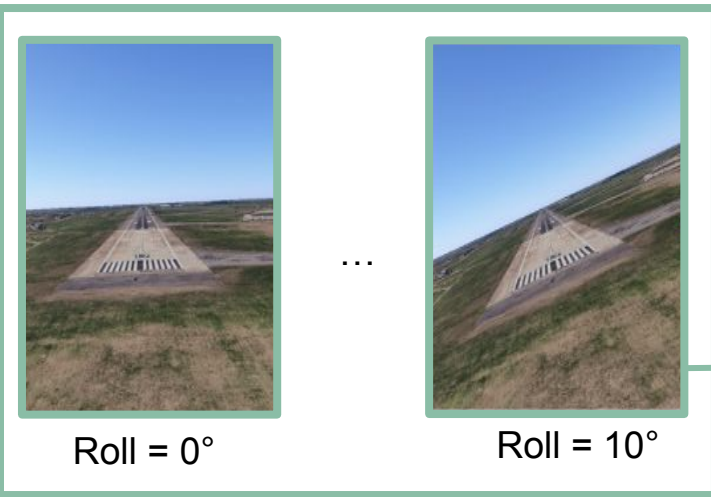
 Verification tools



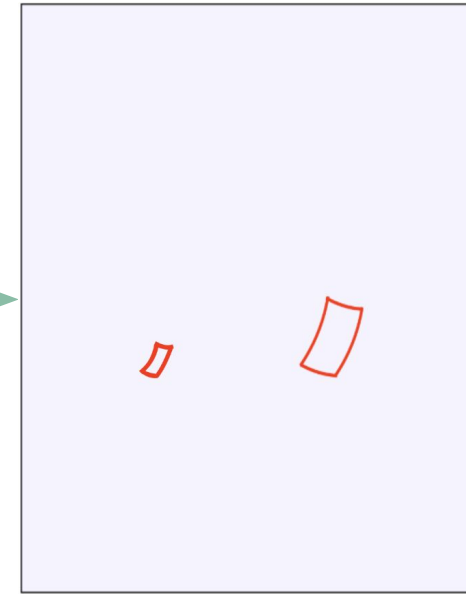


# Formalized property

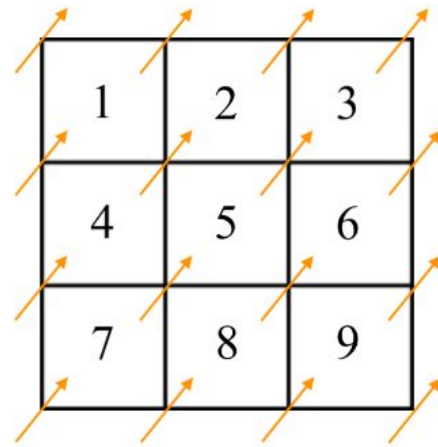
## Mathematical traduction



**Machine learning model**

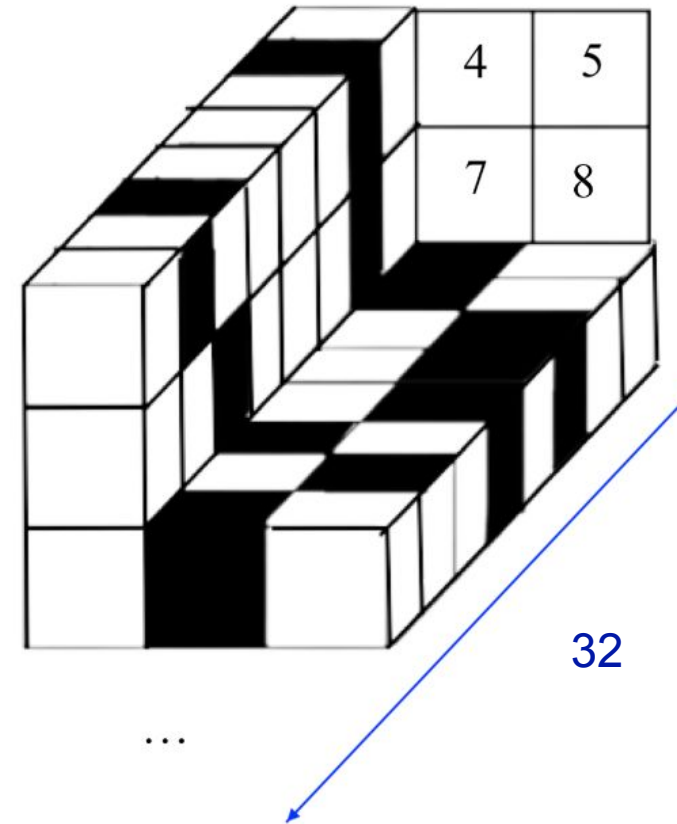


1	2	3
4	5	6
7	8	9



?	4	5
?	7	8
?	?	?

5 pixels unknown in black and white  
32 combinations



- ① Context
- ② Subject

 Neural network

 Property

 Pre/Post-conditions

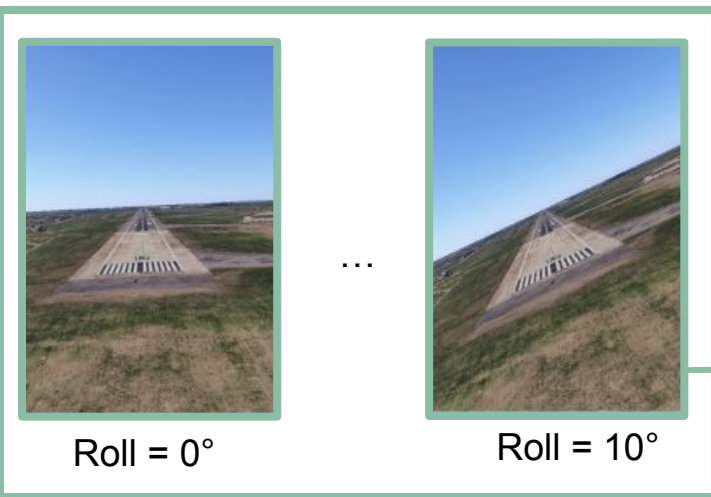
 Formalized property

 Verification tools

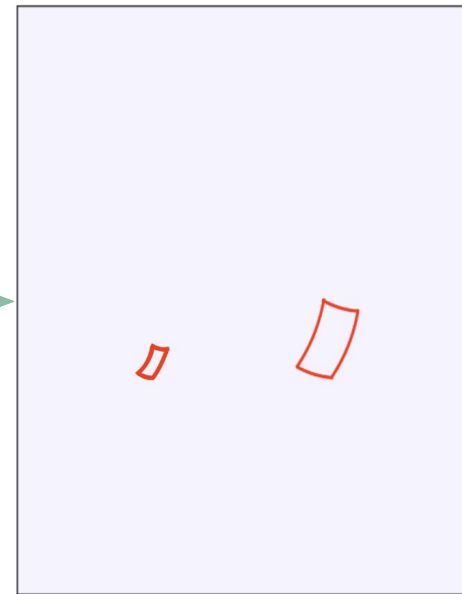


# Formalized property

Mathematical traduction



**Machine learning model**



① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

 **Formalized property**

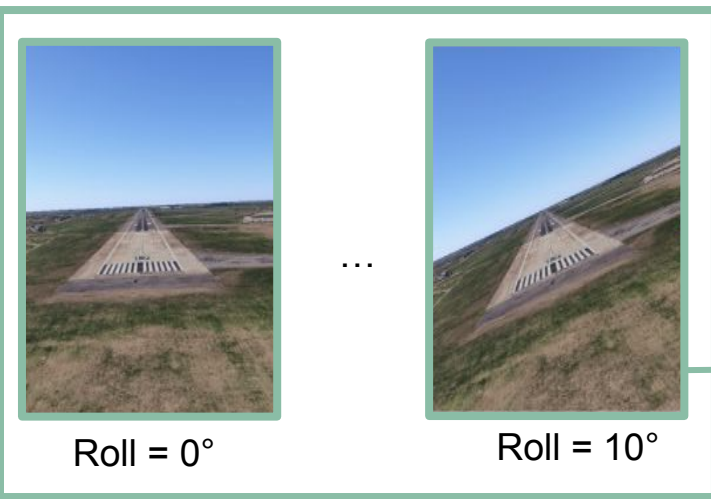
 Verification tools



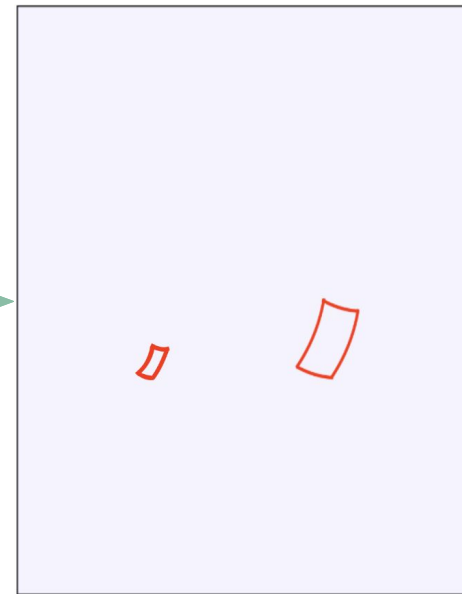


# Formalized property

Mathematical traduction



Machine learning model



- ① Context
- ② Subject

 Neural network

 Property

 Pre/Post-conditions

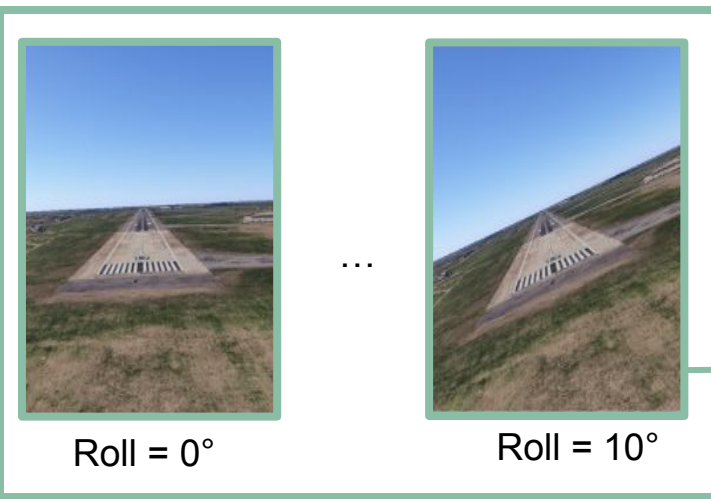
 Formalized property

 Verification tools

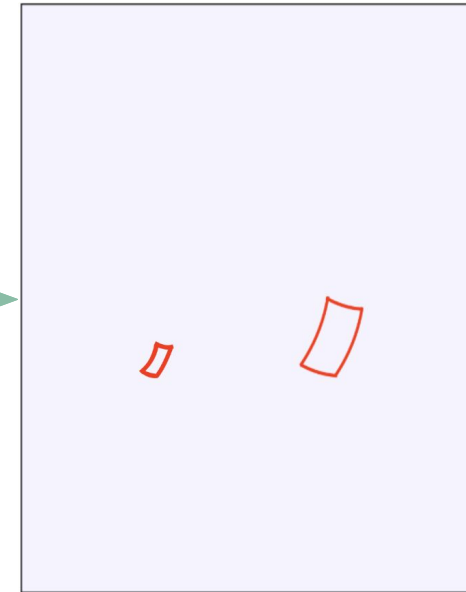


# Formalized property

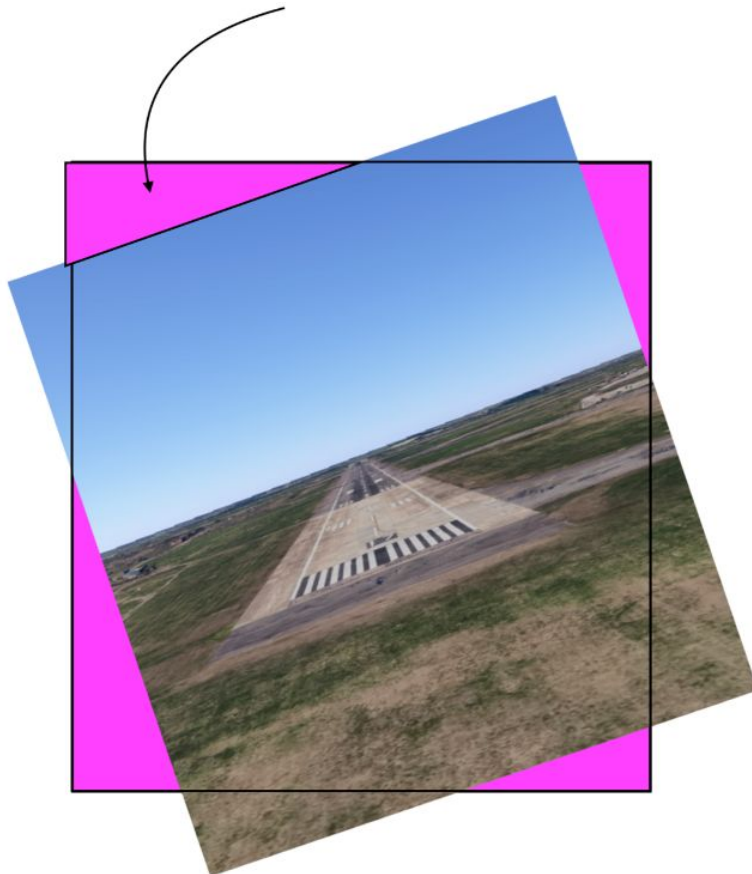
Mathematical traduction



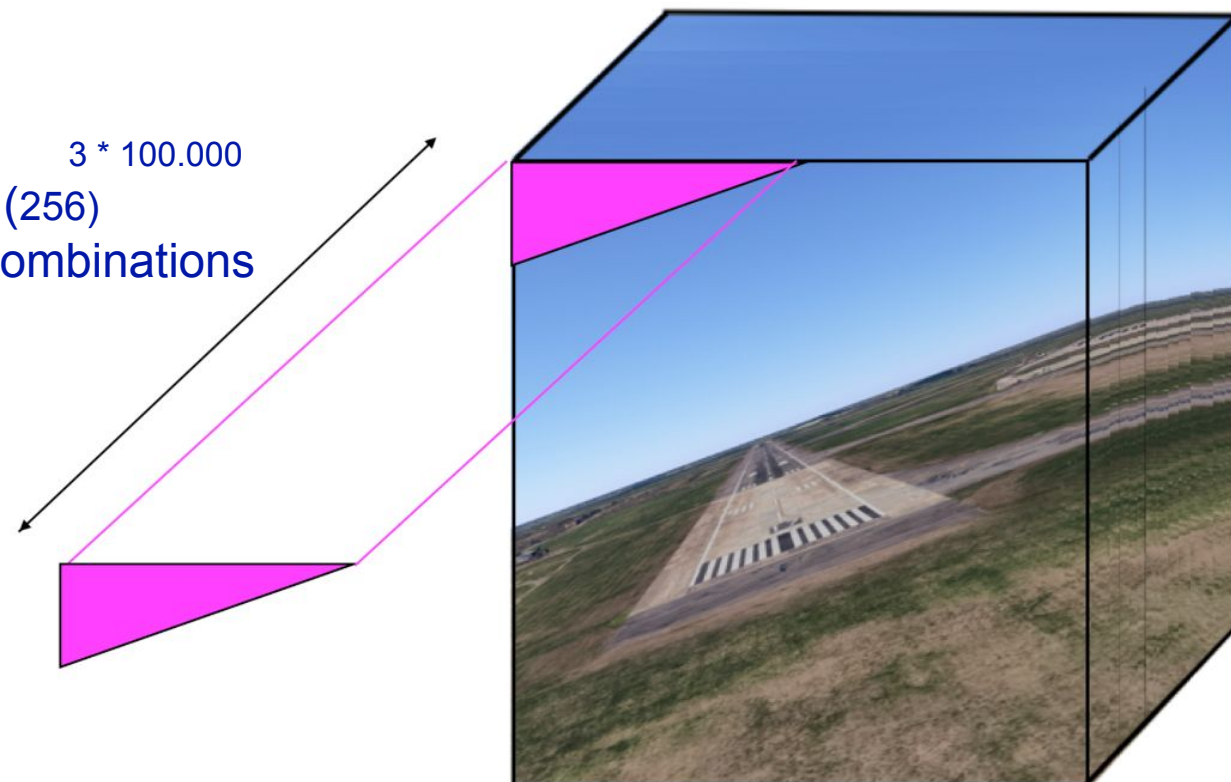
Machine learning model



100.000 unknown pixels in RGB



$3 * 100.000$   
> (256)  
combinations



- ① Context
- ② Subject

 Neural network

 Property

 Pre/Post-conditions

 **Formalized property**

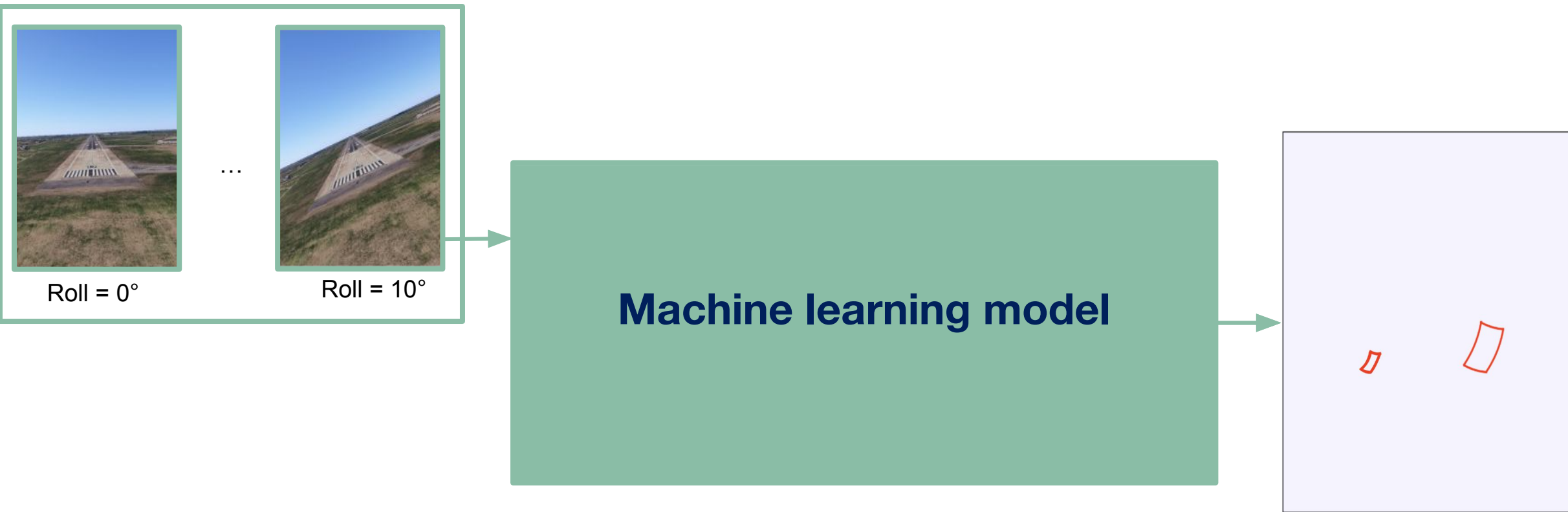
 Verification tools





# Formalized property

Mathematical traduction



Find strategies to reduce dimensionality

① **Context**

② **Subject**

 Neural network

 Property

 Pre/Post-conditions

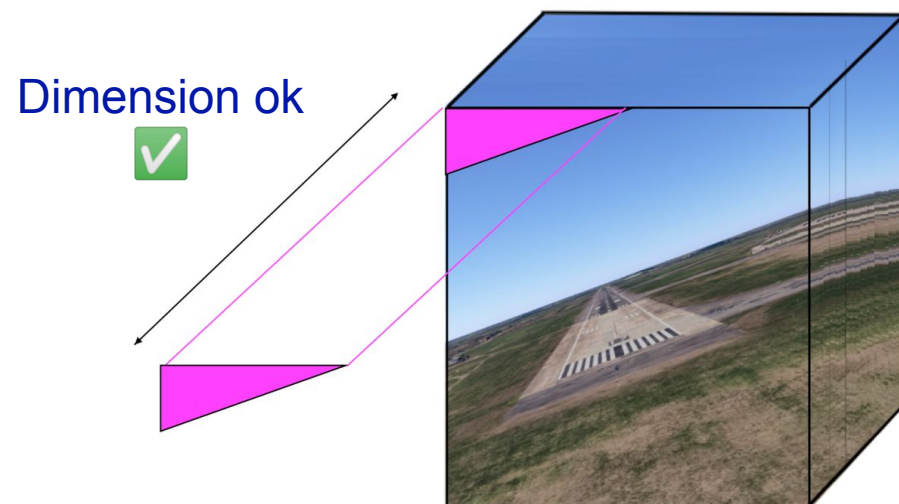
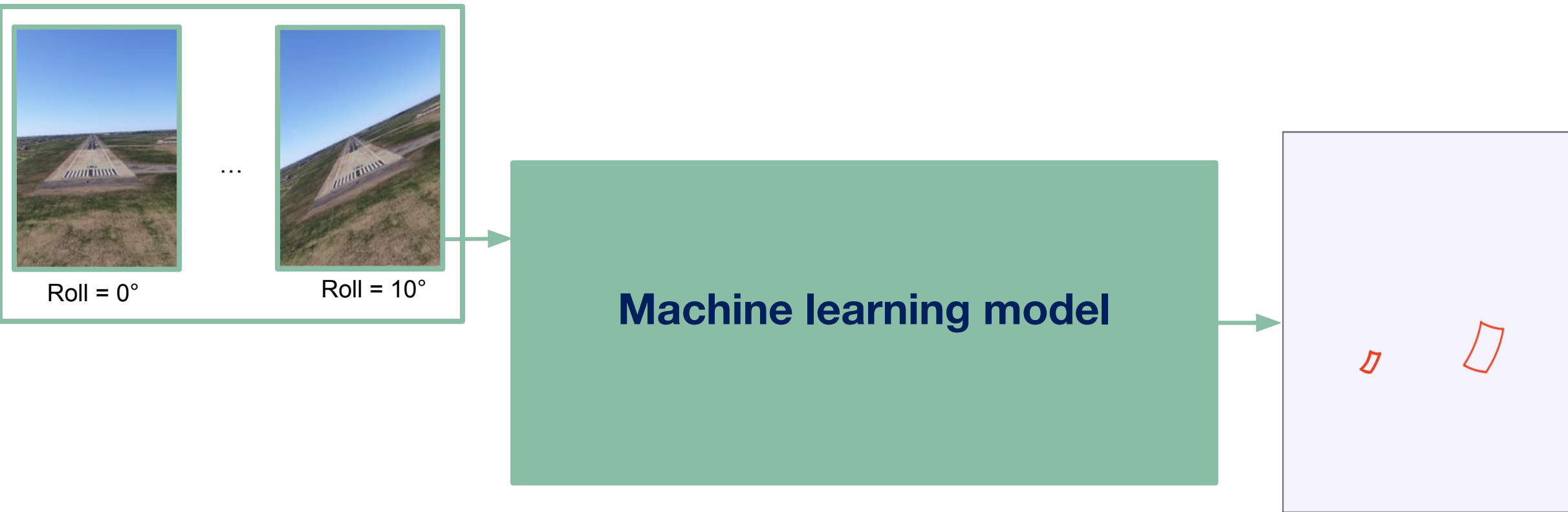
 **Formalized property**

 Verification tools



# Formalized property

Mathematical traduction



Find strategies to reduce dimensionality

① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 **Formalized property**

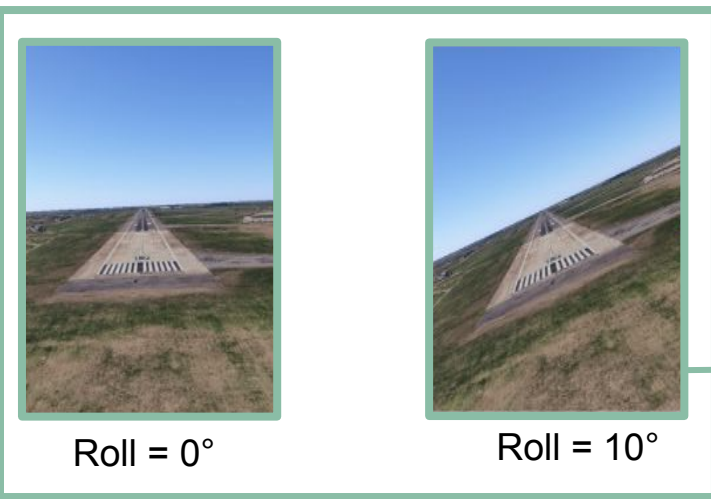
 Verification tools



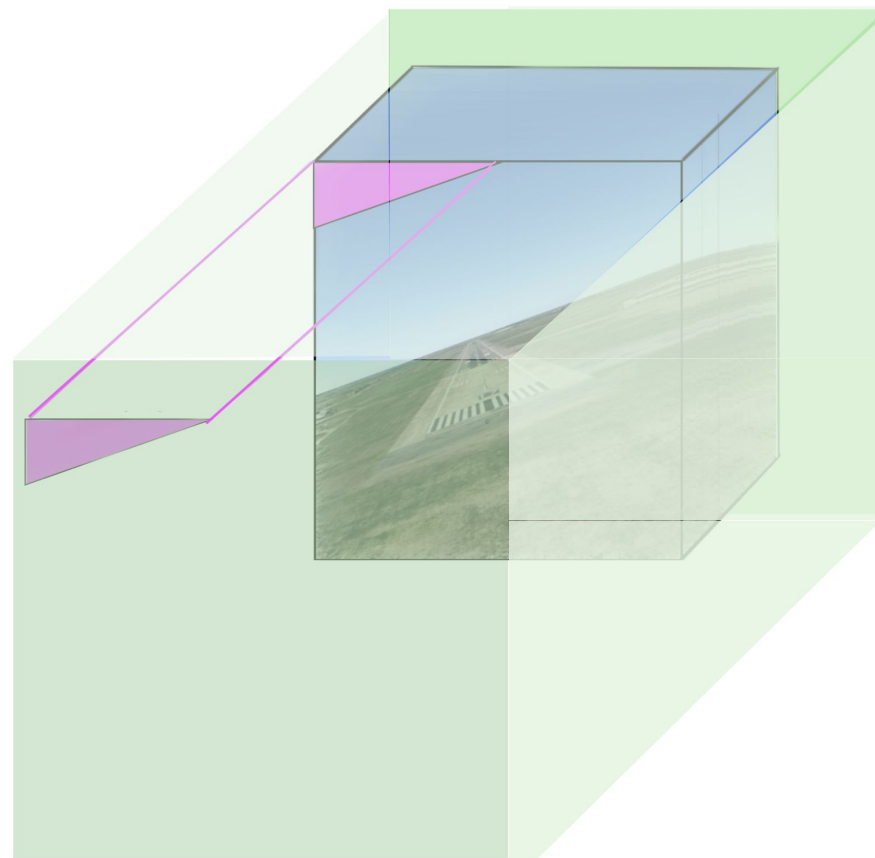
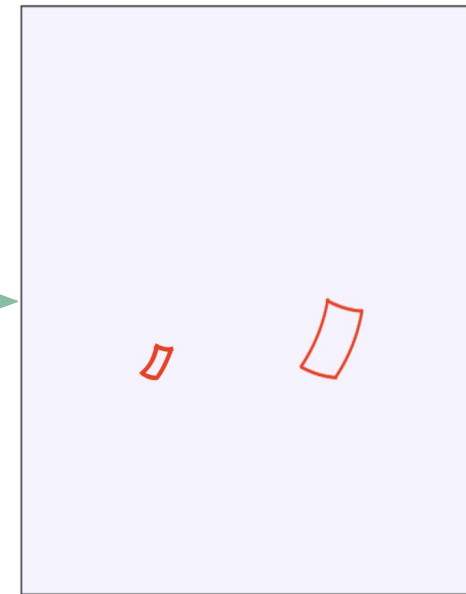


# Formalized property

Mathematical traduction



**Machine learning model**



Creating simplified representation that encompasses all possible cases

*abstraction*

① **Context**

② **Subject**



Neural network



Property



Pre/Post-conditions



**Formalized property**



Verification tools



# Verification tools

Automated validation software

① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

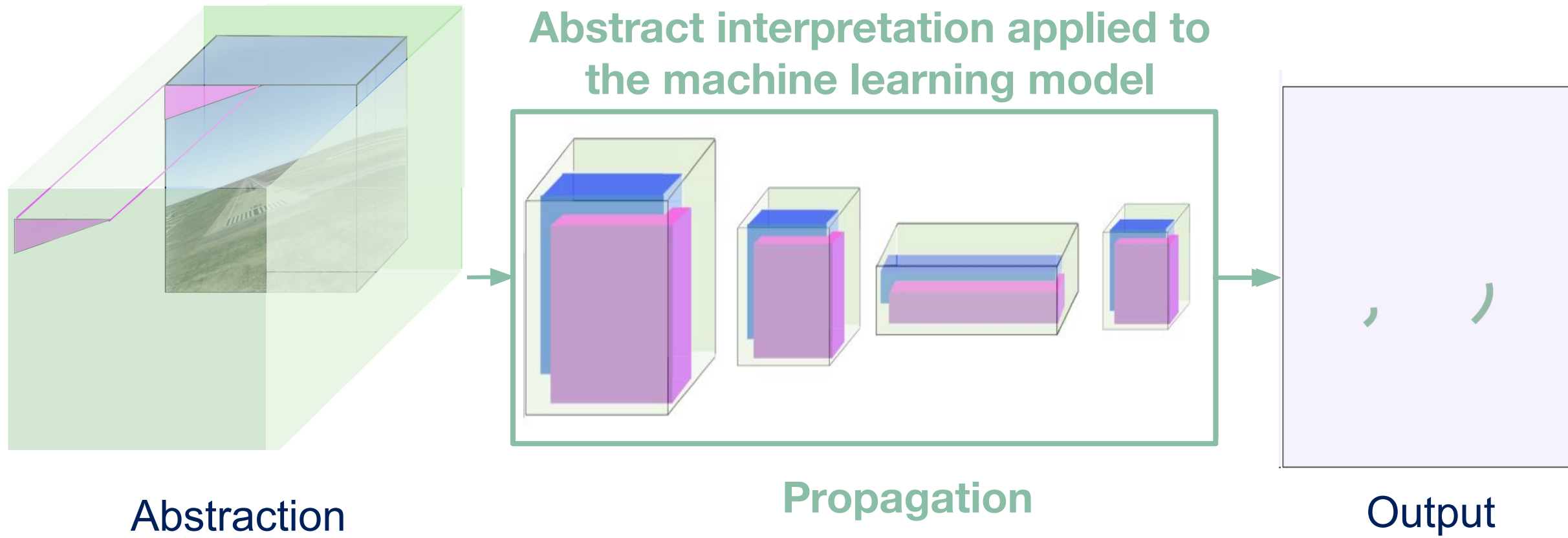
 Verification tools





# Verification tools

Automated validation software



① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

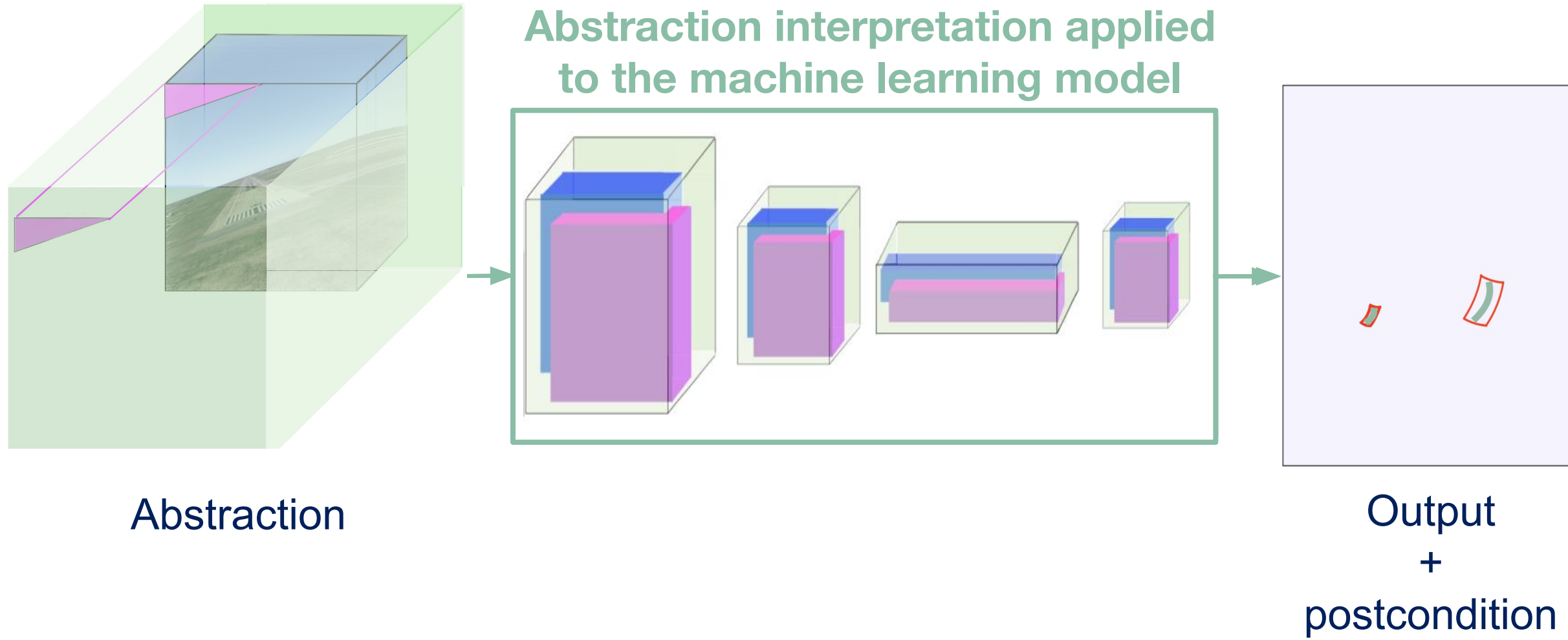
 Formalized property

 Verification tools



# Verification tools

Automated validation software



① Context

② Subject

 Neural network

 Property

 Pre/Post-conditions

 Formalized property

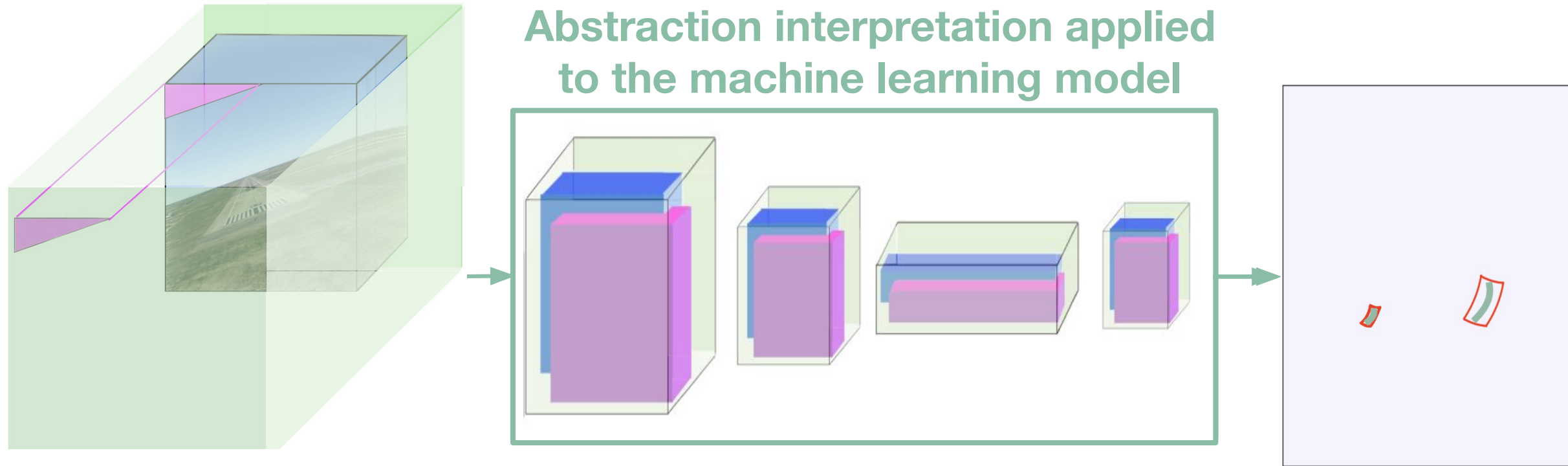
 Verification tools





# Verification tools

Automated validation software



Abstraction

Abstraction interpretation applied to the machine learning model

Output + postcondition

The postcondition is verified for the abstraction

**Verified property**

① Context

② Subject

Neural network

Property

Pre/Post-conditions

Formalized property

Verification tools

# STAKES OF THE SUBJECT

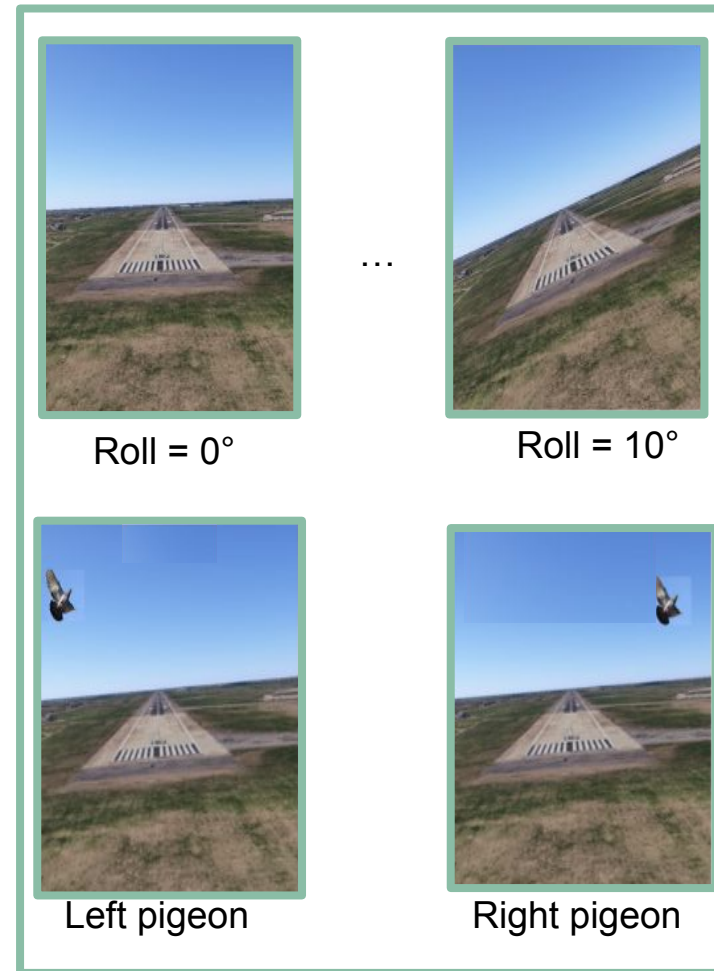




# STAKES OF THE SUBJECT

1

## Not only is the roll set



# STAKES

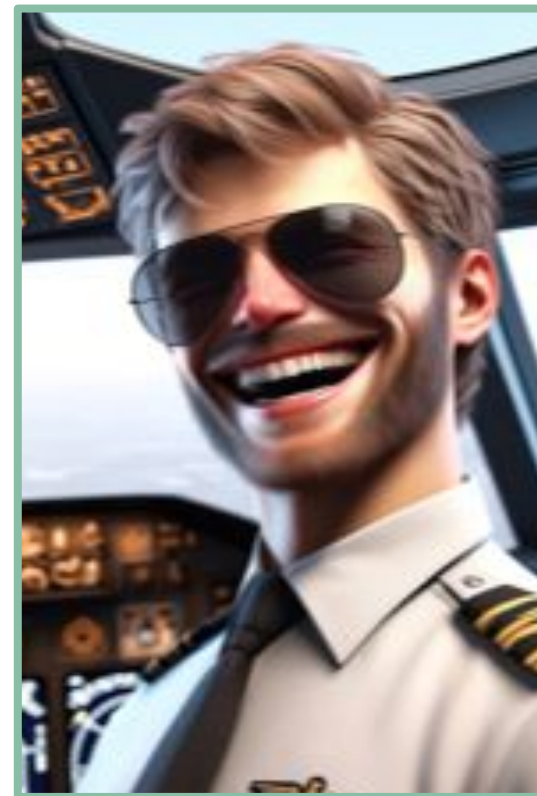
OF THE SUBJECT

1

**Not only is the roll set**

2

**Find properties**



**Danny**



# STAKES

OF THE SUBJECT

- ① **Not only is the roll set**
- ② **Find properties**
- ③ **Abstraction**

# STAKES OF THE SUBJECT

①

**Not only is the roll set**

②

**Find properties**

③

**Abstraction**

④


**Abstract interpretation :**

**Use tools - Use case : Object detection**

**Scalability issue**







# Thank you for your attention

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